

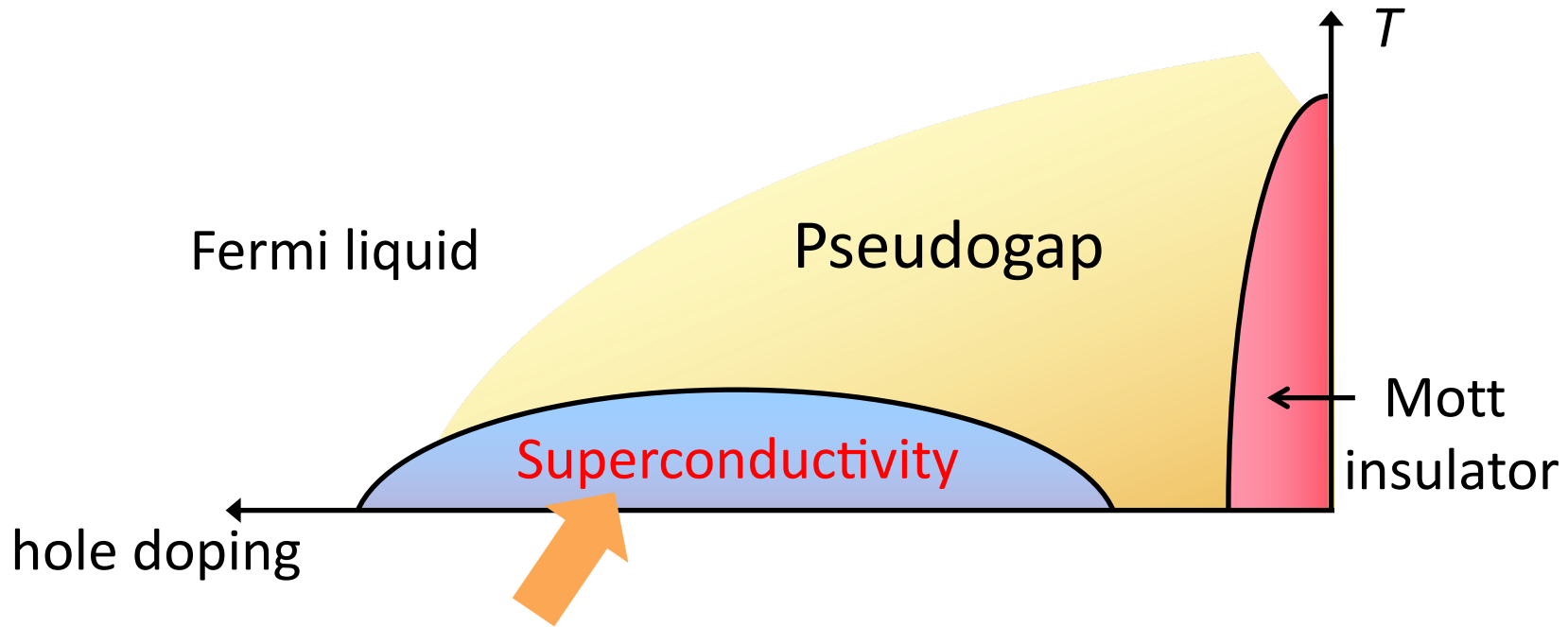
# “s”-wave pseudogap in underdoped cuprates

Shiro Sakai

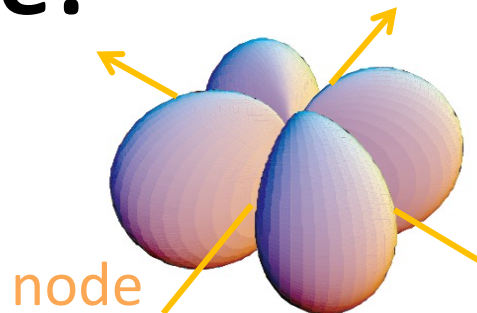
*RIKEN Center for Emergent Matter Science*

S.S., S. Blanc, M. Civelli *et al.*, PRL **111**, 107001 (2013)

# Cuprates are $d$ -wave superconductor



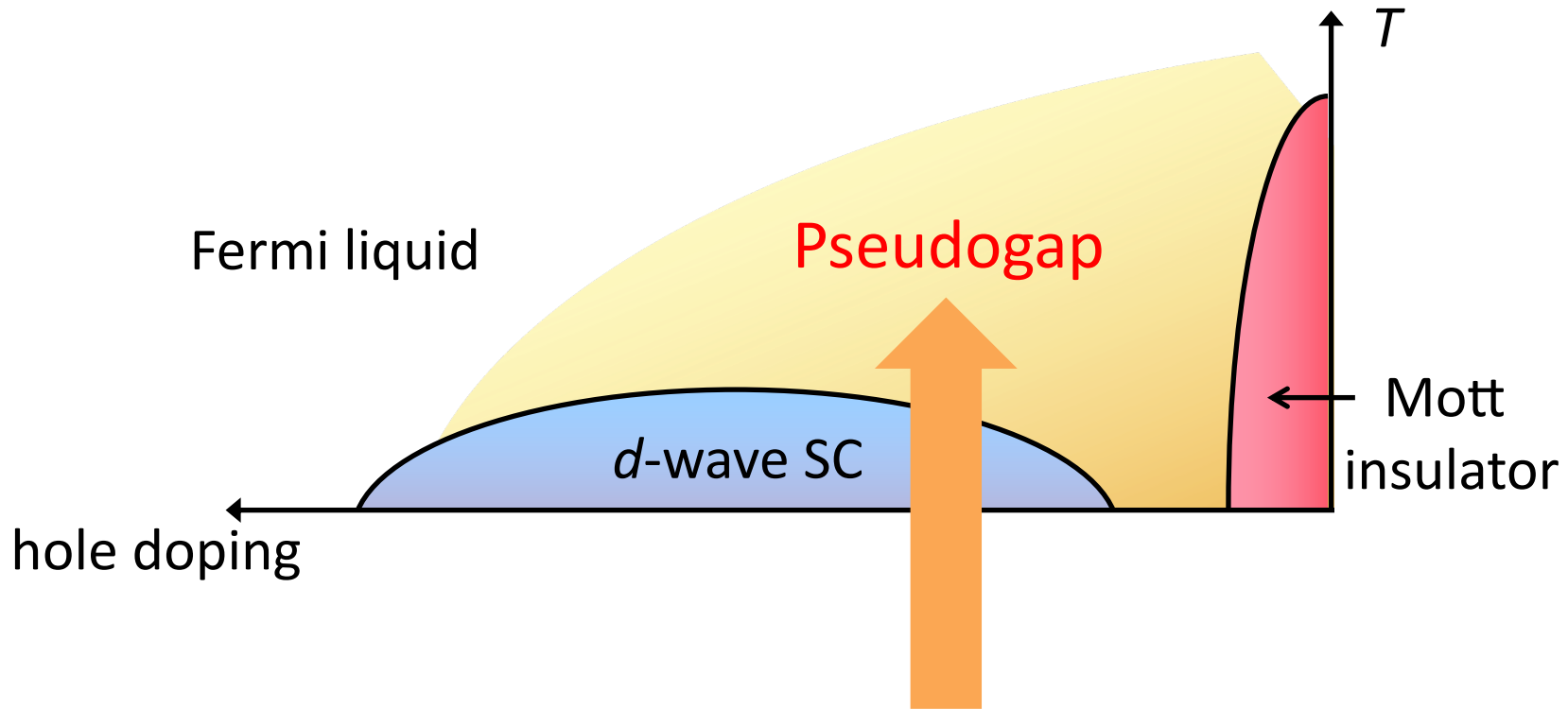
**SC gap is  $d$  wave!**



**Firm evidence  
by SQUID**

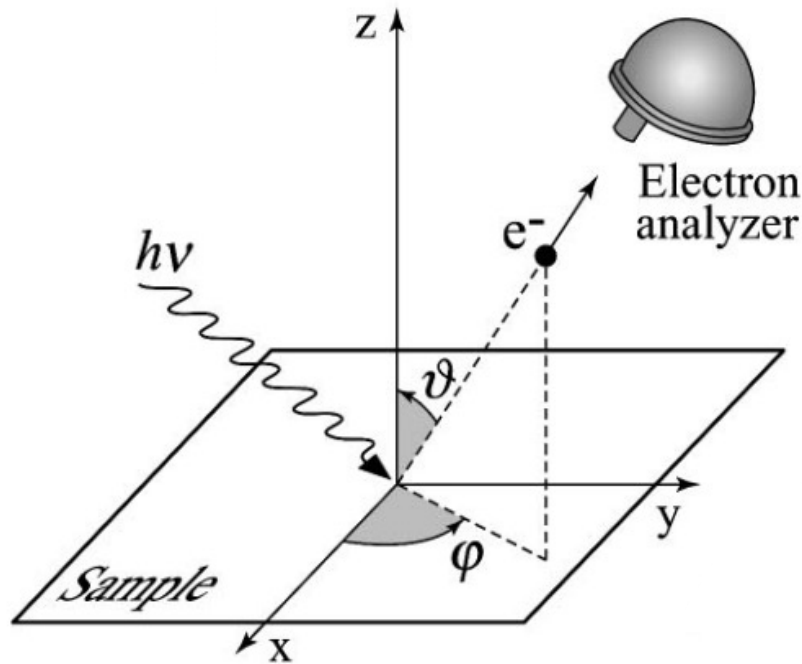
[Wollman *et al.*, PRL'93;  
Tsuei *et al.*, PRL'94]

Pseudogap has been *assumed* to be *d* wave



***No phase-sensitive evidence  
for the pseudogap structure.***

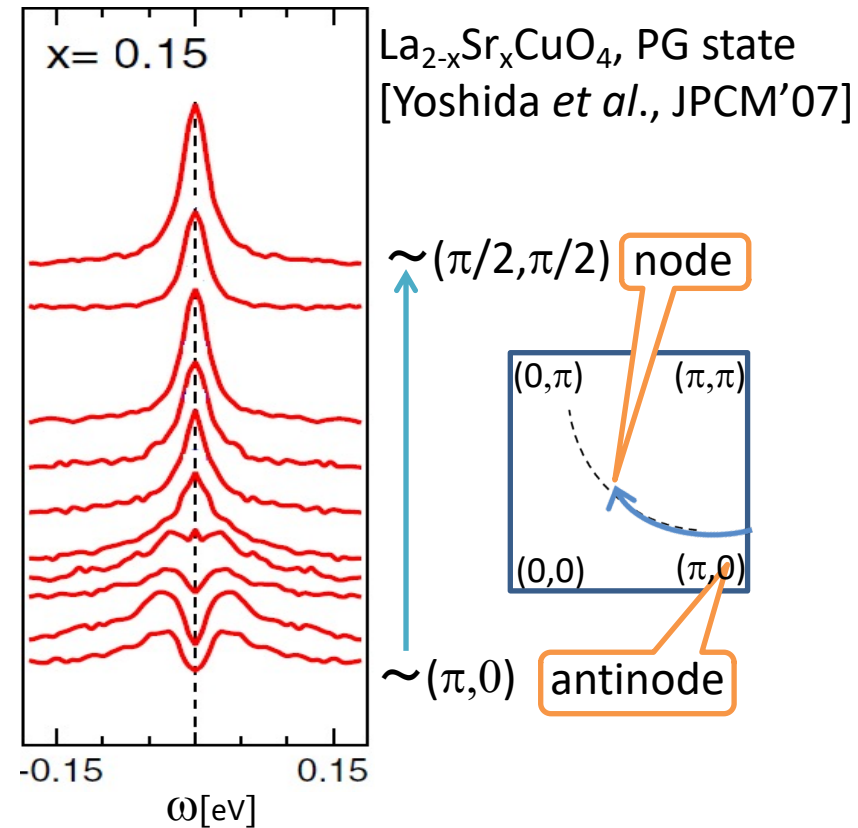
# Pseudogap observed in angle-resolved photoemission spectroscopy (ARPES)



Damascelli, Hussain and Shen, RMP'03

Occupied part of the electronic spectra  $A(\mathbf{k},\omega)$  is measured.

## k-dependent gap

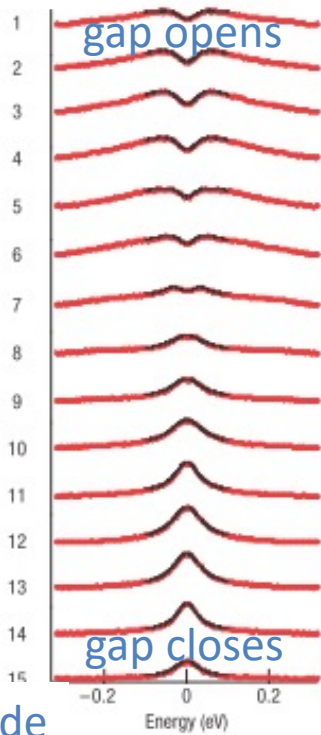


*cf.* Norman *et al.*, Nature'98

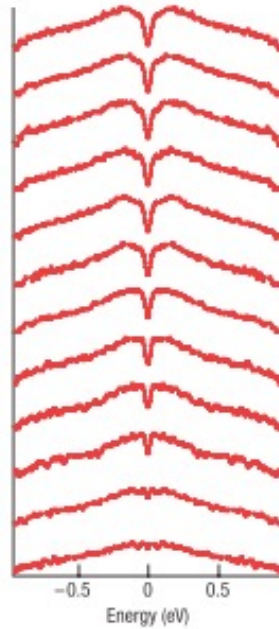
# ARPES “evidence” of *d*-wave pseudogap

According to ARPES,  
*PG* also looks like *d*-wave...

Antinode



$T_c=90\text{K}$ ,  $T=140\text{K}$



$T_c=25\text{K}$ ,  $T=55\text{K}$

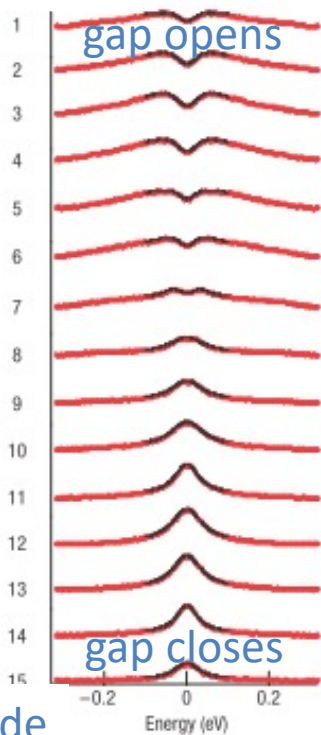
Node

# ARPES “evidence” of *d*-wave pseudogap

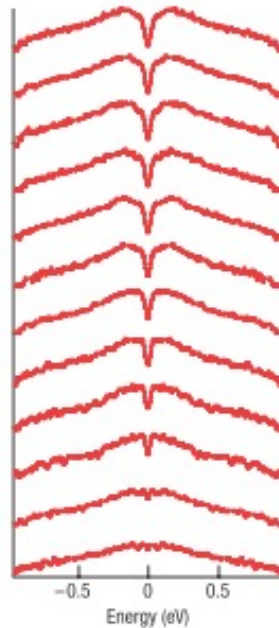
According to ARPES,  
PG also looks like *d*-wave...

But, these are “symmetrized”  
spectra:

Antinode

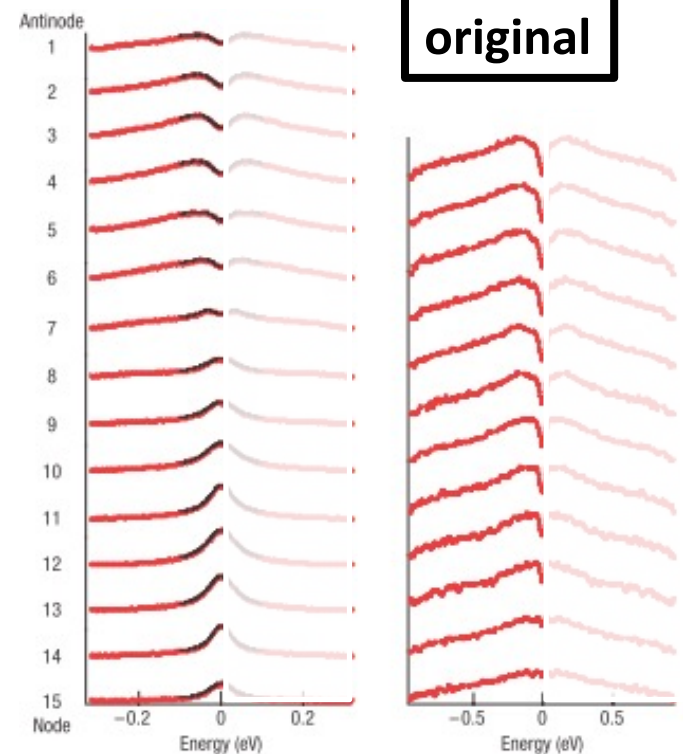


$T_c=90\text{K}$ ,  $T=140\text{K}$



$T_c=25\text{K}$ ,  $T=55\text{K}$

←  
symmetrization



Bi2212 [Figure from Kanigel *et al.*, Nat. Phys.'06]

**Nothing is actually known about above  $E_F$**

# Numerical results

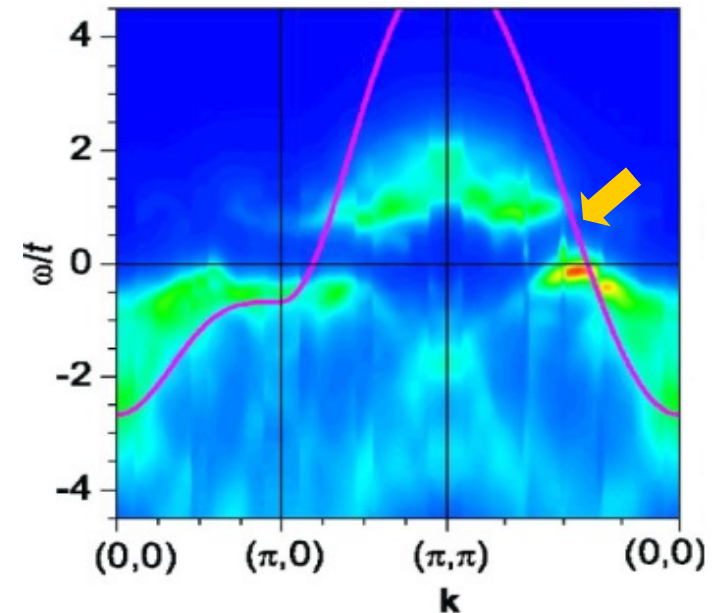
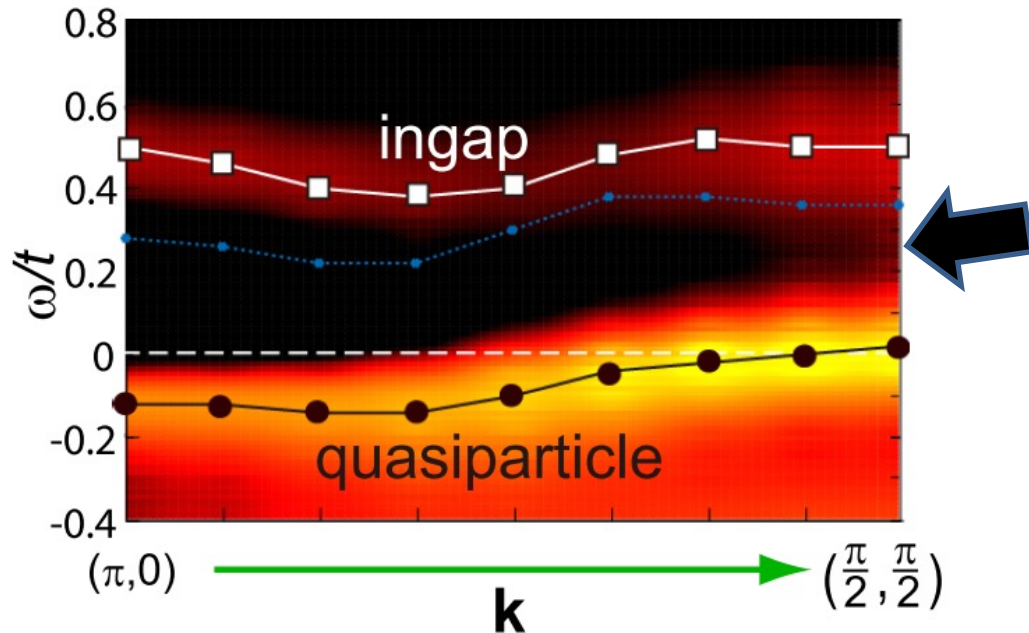
2D Hubbard model (5% doping)

4x4 CDMFT [SS, S. Blanc, M. Civelli *et al.*,  
PRL **111**, 107001 (2013)]

2D  $t$ - $J$  model (10% doping)

20-site exact diagonalization  
[T. Tohyama, PRB **70**, 174517 (2004)]

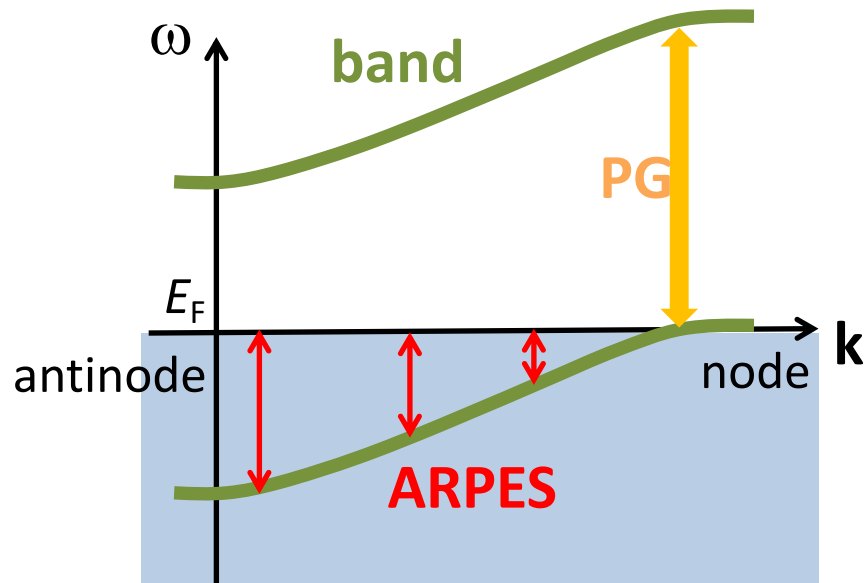
$A(\mathbf{k}, \omega)$



- *Gap opens at every  $k$ .*
  - *Energy position of the gap depends on  $k$ .*
- } **“s”-wave gap**

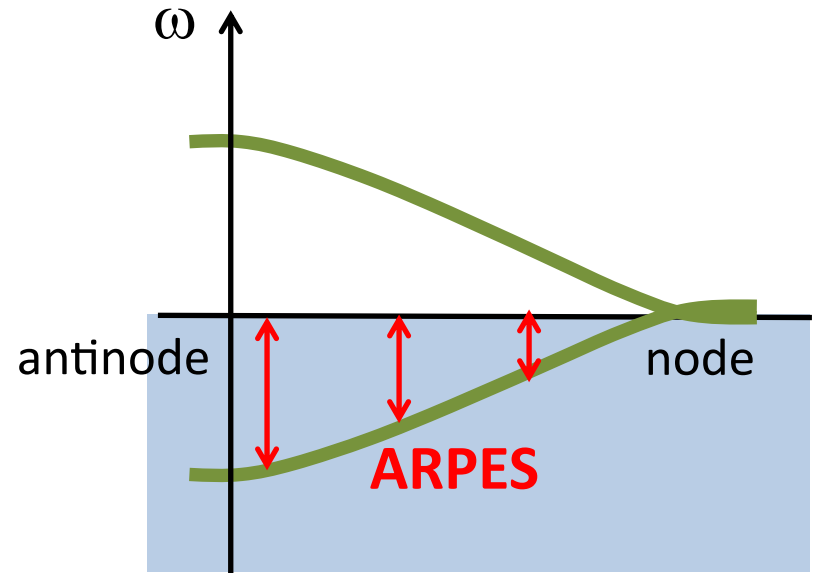
Numerically obtained

**"s"-wave PG**



Often assumed

***d*-wave PG**



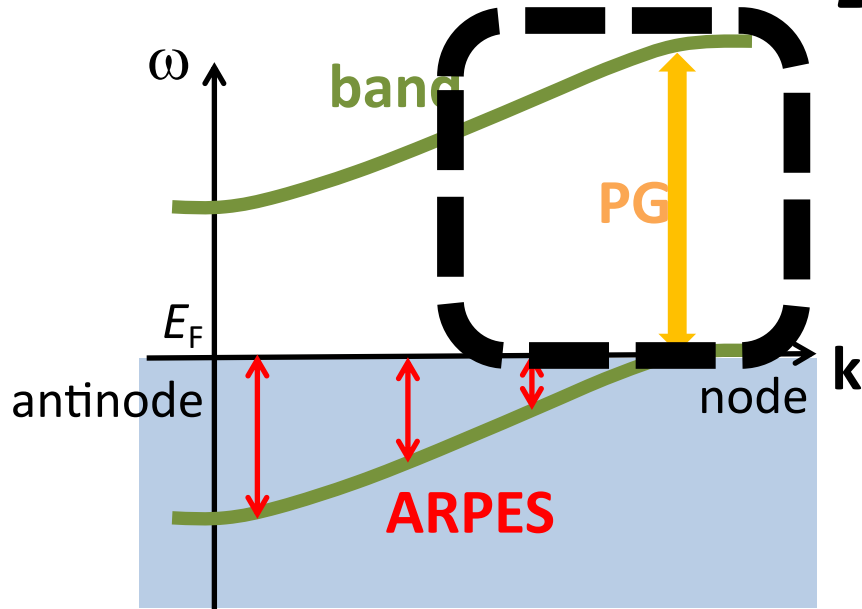
Compared to *d*-wave PG,

- similar below  $E_F$
- different above  $E_F$



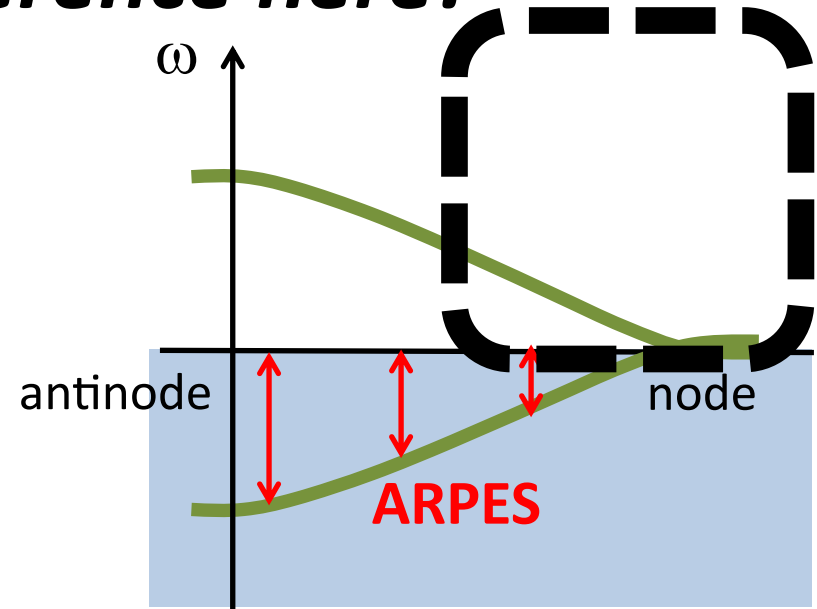
Numerically obtained

**"s"-wave PG**



Often assumed

***d*-wave PG**



***Difference here!***

Compared to *d*-wave PG,

- similar below  $E_F$
- different above  $E_F$

**WANTED**

***Unoccupied spectra in the nodal region for underdoped cuprates***

# **k**-resolved unoccupied spectra are elusive

*Possible in principle by inverse ARPES, though improvement of energy resolution is necessary.*

## **ARPES**

**k**-resolved *occupied* spectra

→ Analysis of high- $T$  data can give information of unoccupied spectra slightly above  $E_F$ .

$$I(\mathbf{k}, \omega) \propto \int A(\mathbf{k}, \omega') f(\omega') R(\omega - \omega') d\omega'$$

## **STM**

**k**-*integrated* occupied and unoccupied spectra.

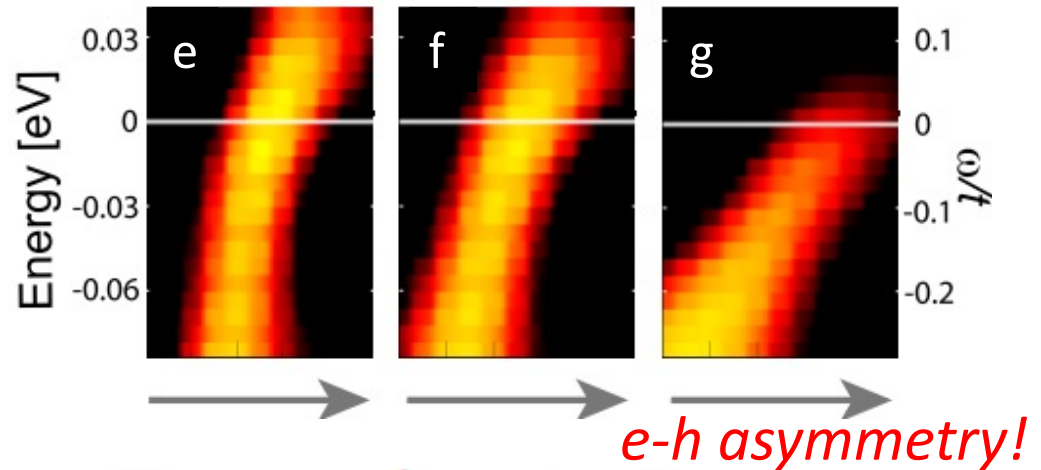
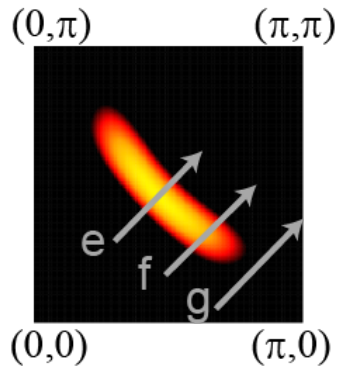
→ A consequence of **k**-resolved spectra can be discussed.

$$\frac{dV}{dI} \sim \text{DOS}(\omega) = \int d\mathbf{k} A(\mathbf{k}, \omega)$$

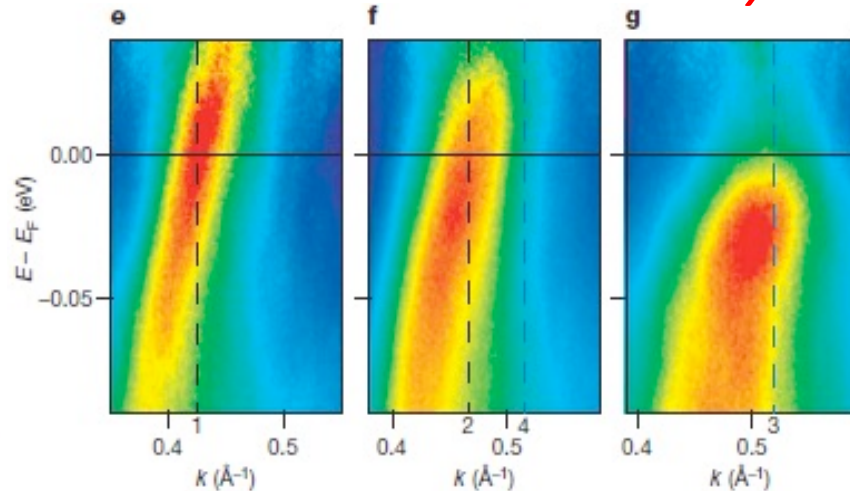
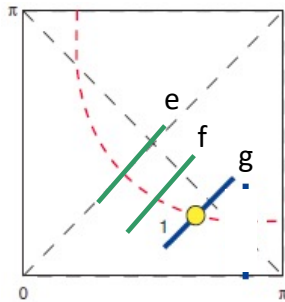
# Indication in ARPES

## CDMFT

$t=0.3eV$   
5% doping  
 $U=8t$   
 $T=0.06t$



## ARPES



Bi2212 (UD65K),  $T=140K$  [Yang et al., Nature'08]

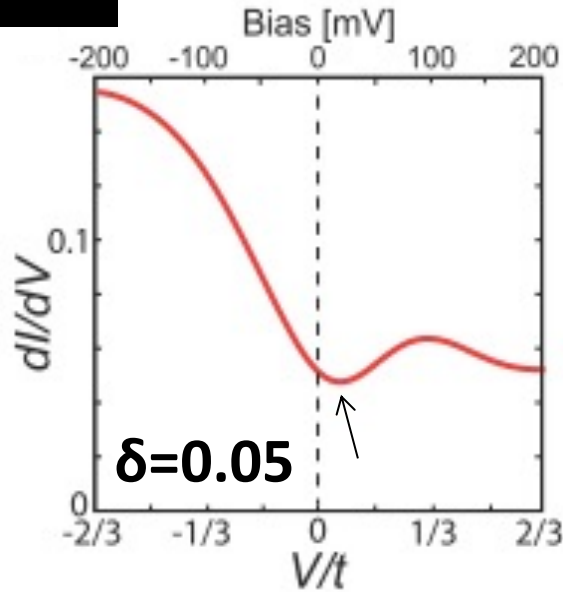
**Analysis of high-T data**

**→ Strong  $e-h$  asymmetry consistent with "s"-wave PG.**

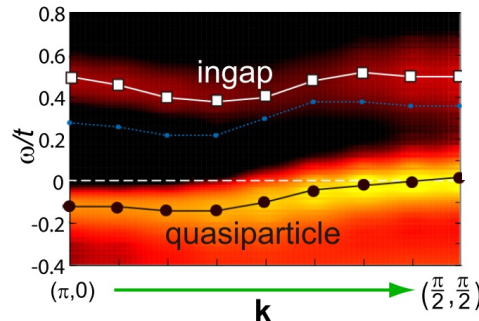
$$I(\mathbf{k},\omega) \propto \int A(\mathbf{k},\omega') f(\omega') R(\omega - \omega') d\omega'$$

# Indication in STM

**CDMFT**

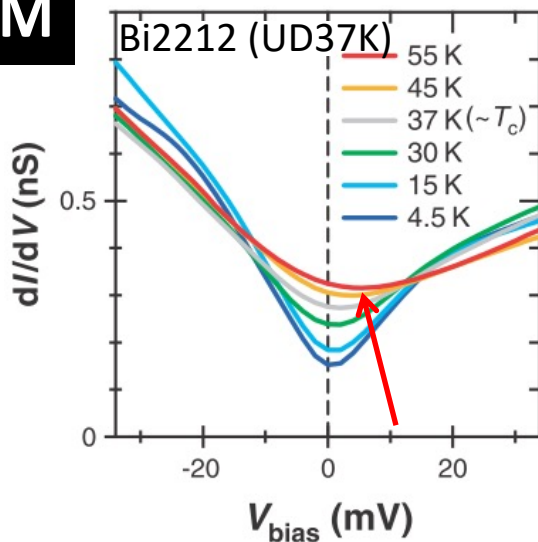


**Bottom shift to positive-energy side**

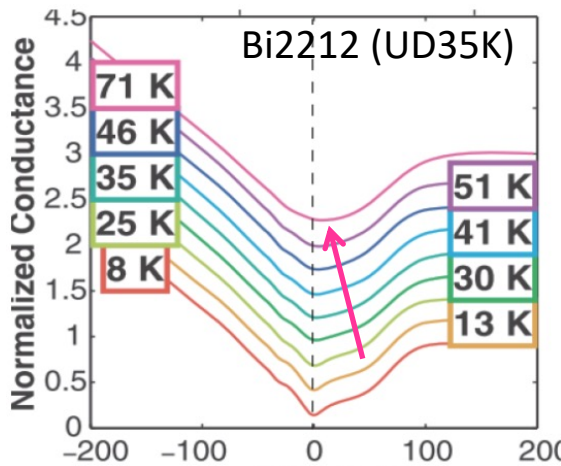


Bottom shift is expected for "s"-wave PG.

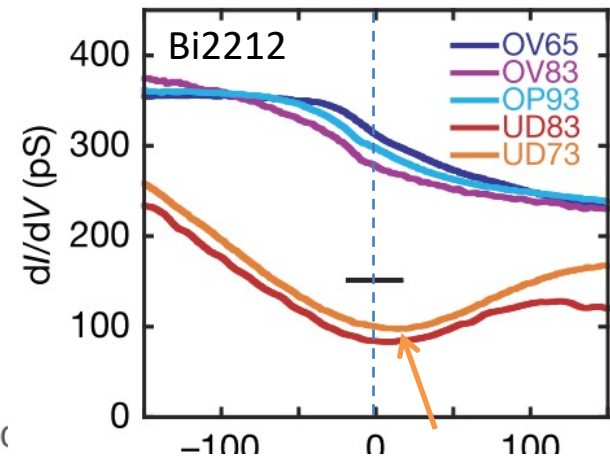
**STM**



[Lee *et al.*, Science'09]



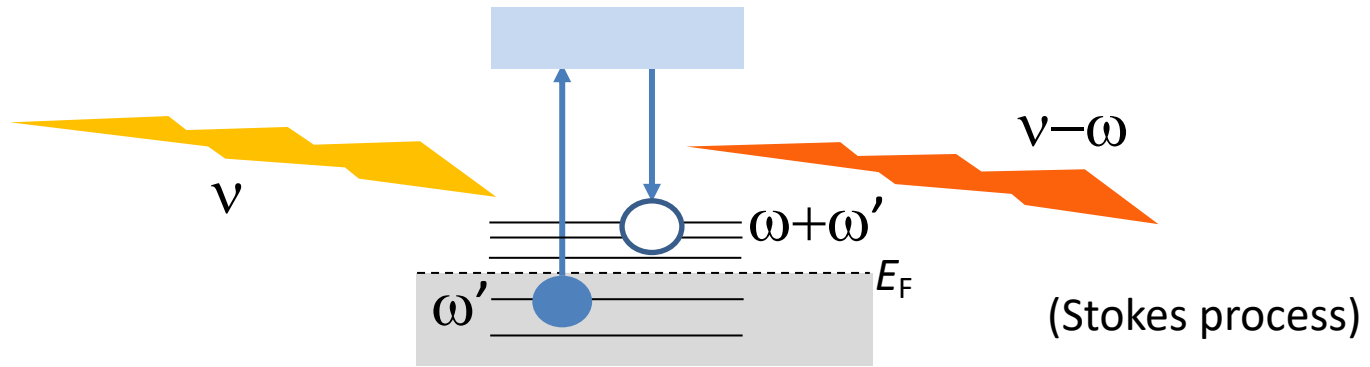
[Pushp *et al.*, Science'09]



[Gomez *et al.*, Nature'07]

**Similar shift in underdoped samples!**

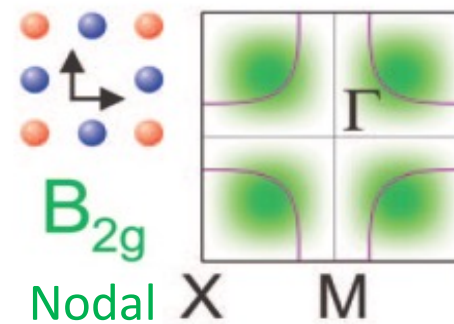
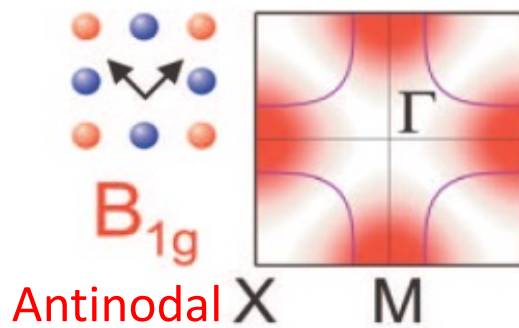
# Electronic Raman Spectroscopy



First approximation:

$$\chi''(\omega) \propto \int d\mathbf{k} \gamma_{\mu}^2(\mathbf{k}) \int d\omega' A(\mathbf{k}, \omega') A(\mathbf{k}, \omega + \omega') [f(\omega') - f(\omega + \omega')]$$

contributed from both occupied and unoccupied spectra.

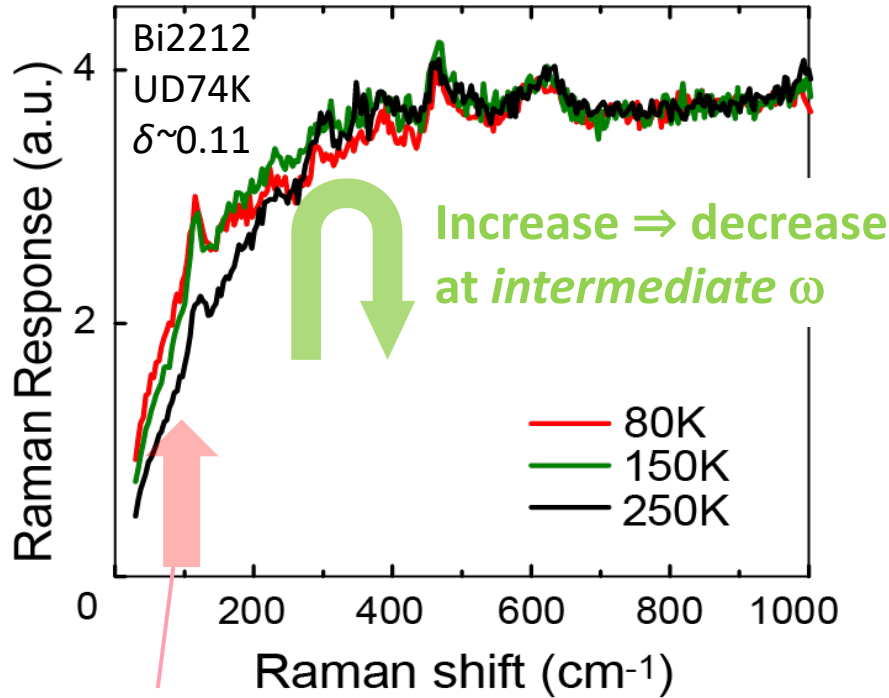


[Devereaux and Hackl, RMP'07]

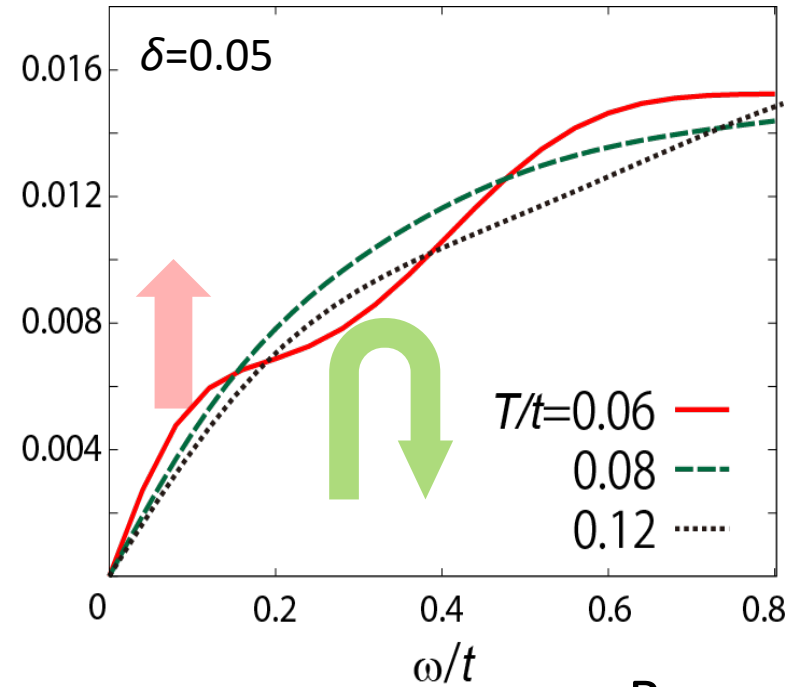
Light polarization gives momentum-space selectivity.

# $B_{2g}$ (nodal) Raman response

## Experiment

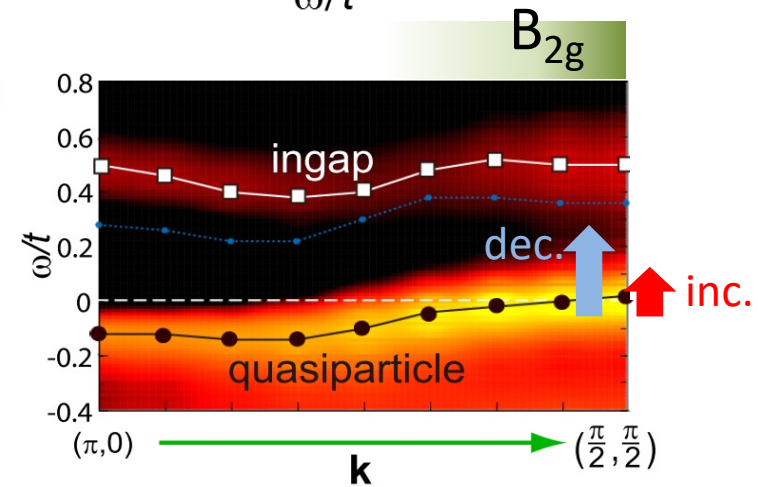


## CDMFT



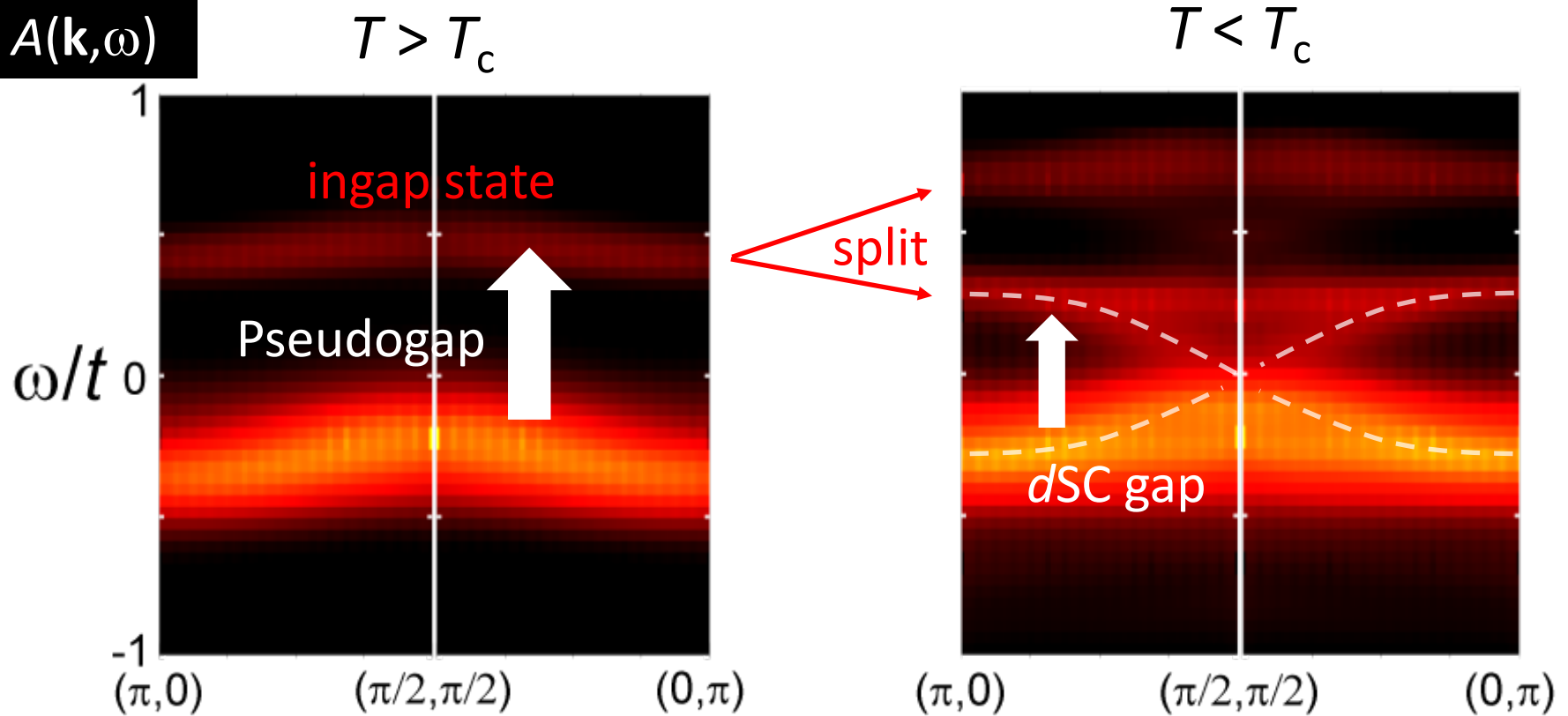
Increases at low  $\omega$ .  
(Metallic behavior)

The intermediate- $\omega$  depression in  $B_{2g}$  Raman signals the gap in the nodal region **above**  $E_F$ .



# How can *s*-wave PG be reconciled with *d*-wave SC?

CDMFT  
 $A(\mathbf{k}, \omega)$



***SC gap appears inside PG!***

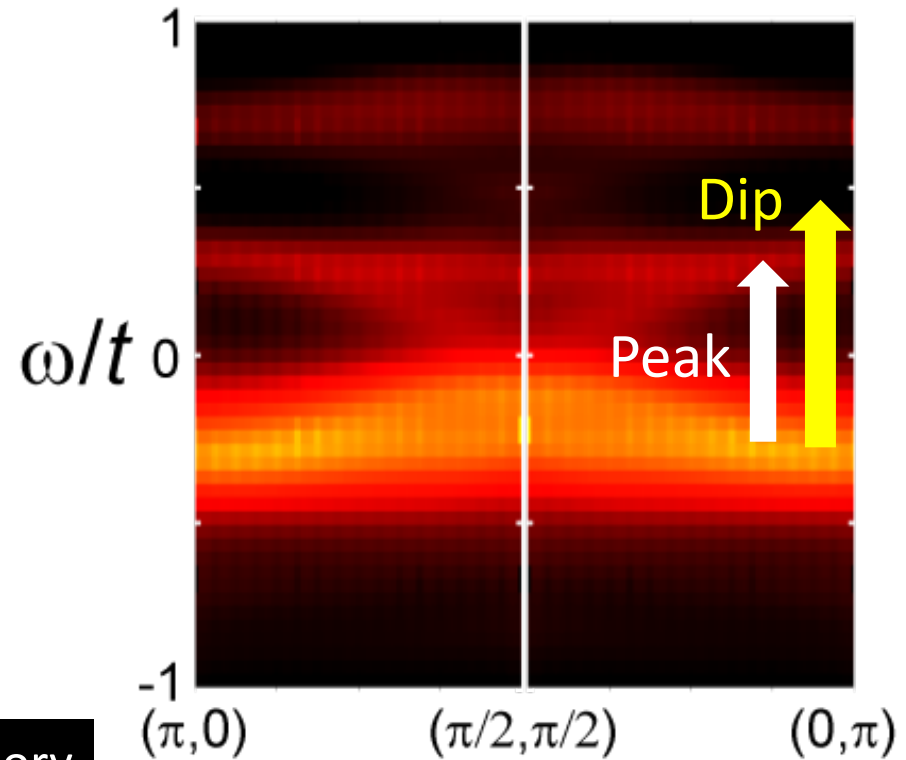
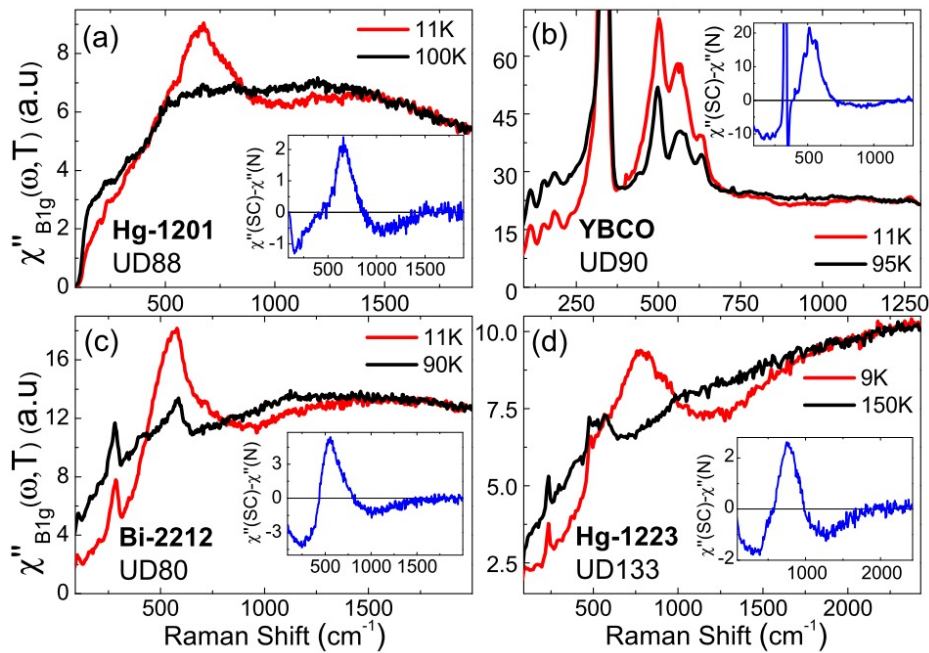
SS, S. Blanc, M. Civelli *et al.*, PRL **111**, 107001 (2013)

SS, M. Civelli, M. Imada, PRL **116**, 057003 (2016).

B. Loret, SS *et al.*, PRL **116**, 197001 (2016)



# Peak-dip structure in $B_{1g}$ Raman response

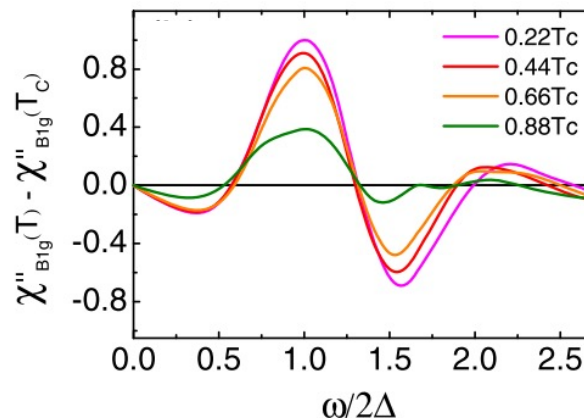
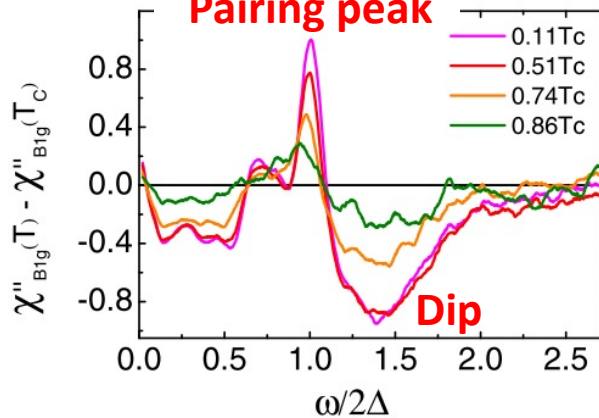


Hg-1223

Experiment

Theory

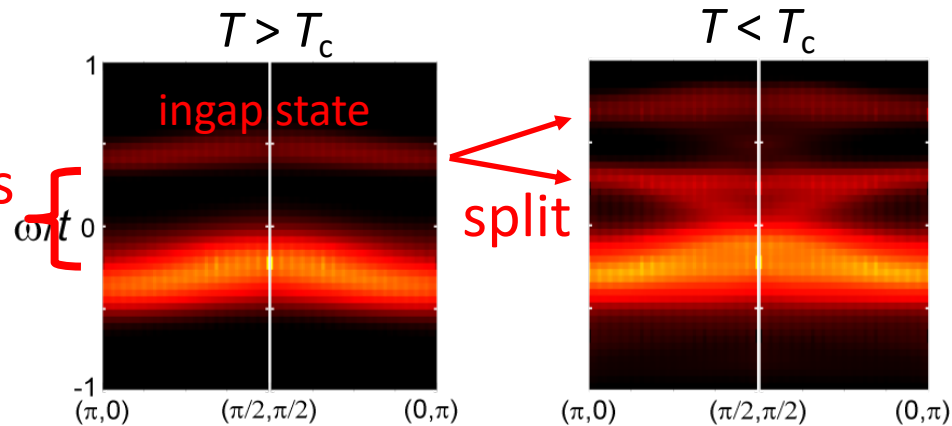
Pairing peak



B. Loret, SS *et al.*,  
PRL **116**, 197001 (2016);  
PRB **96**, 094525 (2017)



Strong scattering is present inside PG



- *Why and how does the ingap peak split?*
- *Under the strong scattering due to PG, how can the Bogoliubov peaks emerge?*

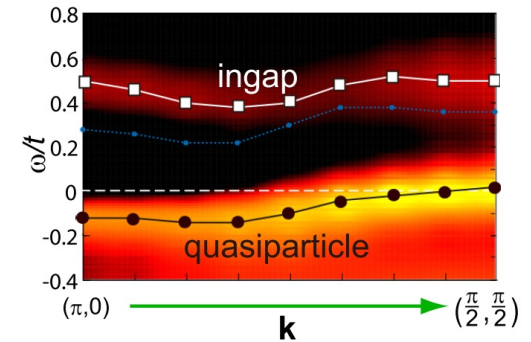


- *Below  $T_c$ , the scattering (normal self-energy) is **cancelled out** by a contribution from anomalous self-energy.*

# Summary

## “s”-wave pseudogap

- Finite gap even at the node but **above**  $E_F$ .
- The gap below  $E_F$  is *d*-wave like.



	<i>d</i> -wave PG	“s”-wave PG
Numerical simulation (2D Hubbard, t-J)		✓
ARPES (occupied spectra)	✓	✓
ARPES (E-h asymmetry)		✓
STM (E-h asymmetry)		✓
$B_{2g}$ Raman (Finite-energy dip)		✓
$B_{1g}$ Raman	✓	✓